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$$\mu_{\bar{x}} = \mu_x \quad \text{and} \quad \sigma_{\bar{x}} = \sigma_x \cdot \frac{1}{\sqrt{n}} \sqrt{\frac{N-n}{N-1}}$$

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