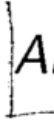


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# Arithmetic and Geometry

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*Ten Years in*  *Alpbach*

EDITED BY

Gisbert Wüstholz and Clemens Fuchs

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